

A close-up photograph of a person's hands working on a desk. The left hand holds a magnifying glass over a sheet of paper covered in a dense, repeating pattern of small, stylized symbols. The right hand holds a pen, poised to write on an open notebook. The notebook has some faint, handwritten notes. The scene is dimly lit, with a strong light source creating highlights on the paper and the person's skin. The overall atmosphere is one of focused investigation or research.

Cryptography Algorithms

CMPT 201

Slides 12.1

Based on content
created by Dr. Steve Ko
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Topics

- What is **cryptography**?
- What are the **basics of cryptographic algorithms**?
 - What are **cryptographic hashes**?
 - What is a **secret key encryption**?
 - What is **public-key encryption**?

Cryptography: The absolute basics

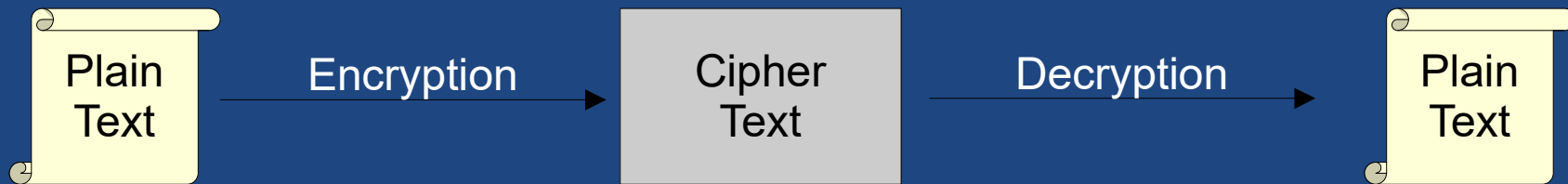
Context

- **Cryptography**
 - A very broad area.
 - We'll focus on how to use cryptography.
 - We just touch on the basics!

The CIA Model

- CIA model: the classic security model.
 - Confidentiality:
..
 - Integrity:
..
and only by authorized parties.
 - Availability:
..
- Threat examples
 - Against confidentiality: classified information leak
 - Against integrity: fake images/videos
 - Against availability: Denial-of-Service (DoS) attacks

General Cryptography Process



- Cryptographers invented secret codes to hide messages from unauthorized observers.
- **Challenges:**
 - How can you **hide** a message from everyone but the intended recipient?
 - How can the recipient know the message is **authentic**?

ABCD: Traditional Cryptography

- **Traditional Cryptography:**
 - Secret codes, which are secret algorithms.
 - E.g., Caesar Cipher: ..

For +1 'A' becomes 'B'.

- **ABCD:** Which of the following is the **cipher text** from using a **3-letter shift Caesar Cipher** on the plain text “**Hello world**”?

- a) EBIIL TLOIA
- b) KH00R ZRU0G
- c) IFMMP XPSME
- d) LOW0R LDHEL

- **What is the problem with a secret algorithm?**
 - When your algorithm (or code book) is compromised,
..

Modern Encryption

- Algorithms are Public
 - ..
 - May be symmetric (secret key) or asymmetric (public key).
- Why is this better?
 - If algorithm or code is secret, then if it falls into the wrong hands it means code is useless.
 - If only key is private, then if it falls into the wrong hands then ..

Crypto Algorithm Goals

- Choose an encryption algorithm such that:
 - Given a key, it should be
..
 - Without a key, it should be
..
- Strength of security often based on length of key:
Longer key is more difficult to guess (by brute-force).

Window of Validity

- Window of Validity

..

- Must only use algorithm that have not been compromised.

- Problem:

Window of validity of your crypto function

..

- Design systems so you can replace the crypto function easily.

- Example Windows of Validity

- 1993: SHA-0 was published.
- 1995: Possible weakness was found in the SHA-0 algorithm; replaced with SHA-1.
- 2004: Published way to compromise SHA-0
- 2017: Published way to compromise SHA-1
- ????: Published way to compromise SHA-256?

Three Types

- Types of cryptography algorithms based on their keys:
 - Zero keys: ..
 - One key: ..
 - Two keys: ..

Cryptographic Hash Functions (Zero Keys)

Cryptographic Hash Functions

- Suppose we have a cryptographic hash function $h()$
 - It takes a message m of arbitrary length as input and
 - ..

- Toy example:
 $h(m) = (m^2) \% 4321$

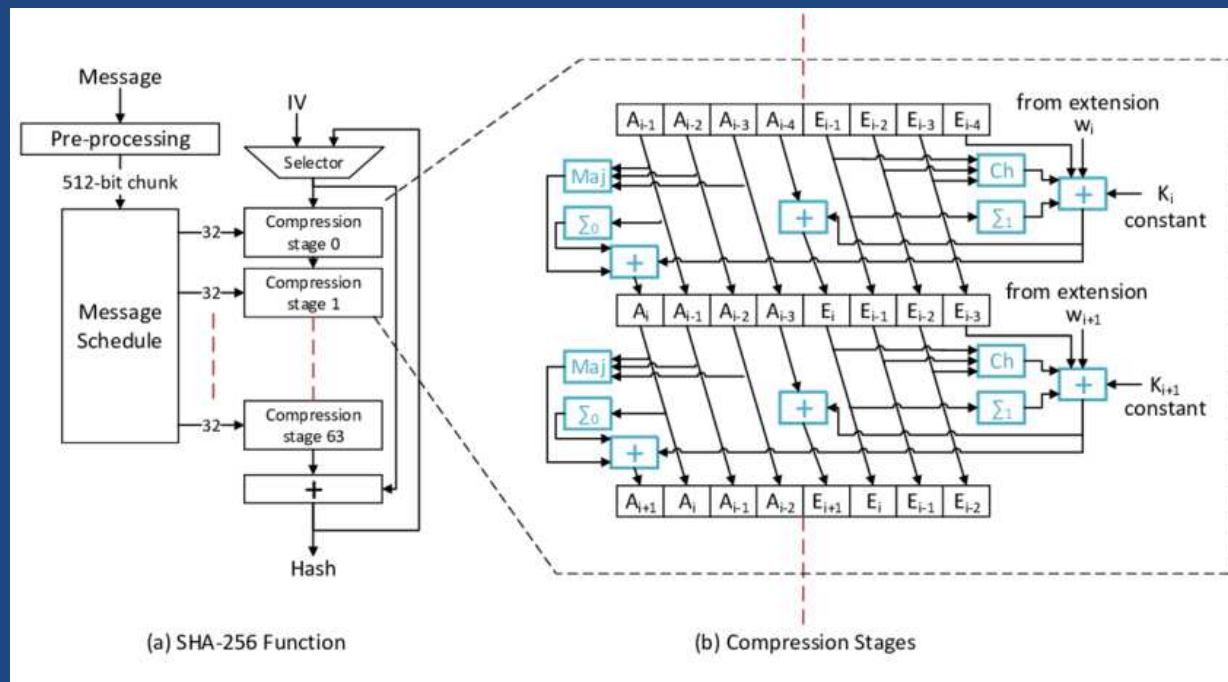
m	m in hex		h(m)
AAAA	(0x41414141)	-->	2242
BBBB	(0x42424242)	-->	893
CCCC	(0x43434343)	-->	2558
DDDD	(0x44444444)	-->	2916
EEEE	(0x45454545)	-->	1967
FFFF	(0x46464646)	-->	4032
GGGG	(0x47474747)	-->	469
HHHH	(0x48484848)	-->	4241
IIII	(0x49494949)	-->	2385
JJJJ	(0x4A4A4A4A)	-->	3543
KKKK	(0x4B4B4B4B)	-->	3394
LLLL	(0x4C4C4C4C)	-->	1938

Hash Function Properties

- ..
 - It should be easy to compute $h(m)$
- ..
 - Given $h(x)$, it should be difficult to find x .
 - i.e., the reverse of $h()$ should be difficult to compute.
- ..
 - Given x , it should be difficult to find x' where $h(x') == h(x)$
 - i.e., Given a value and a hash function, it should be difficult to find another value that produces the same hash.
- ..
 - It should be difficult to find two messages x and x' where $h(x) == h(x')$
 - i.e., given a hash function, it should be difficult to find any two values that produce the same hash.

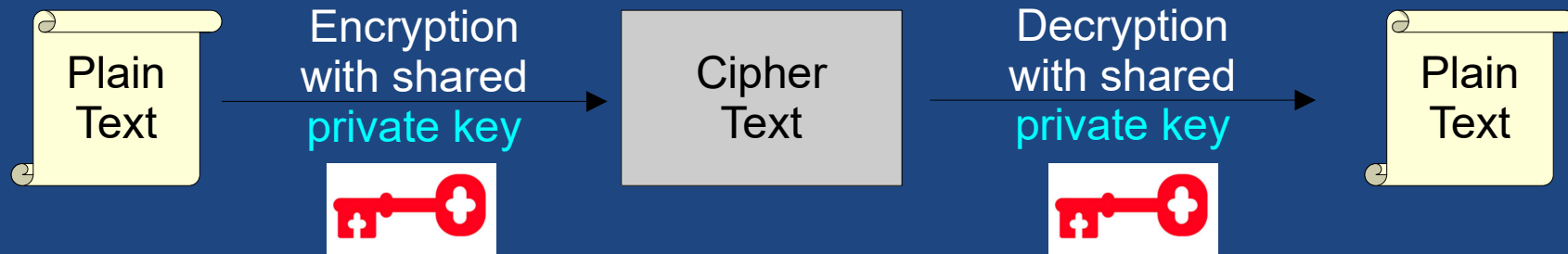
Ideal Hash

- Ideally, we want all these properties for a strong cryptographic hash function.
 - However, not all hash functions provide all these properties.
- Example good crypto hash function: SHA-256.



Private Key Cryptography or Symetric Key Cryptography (One key)

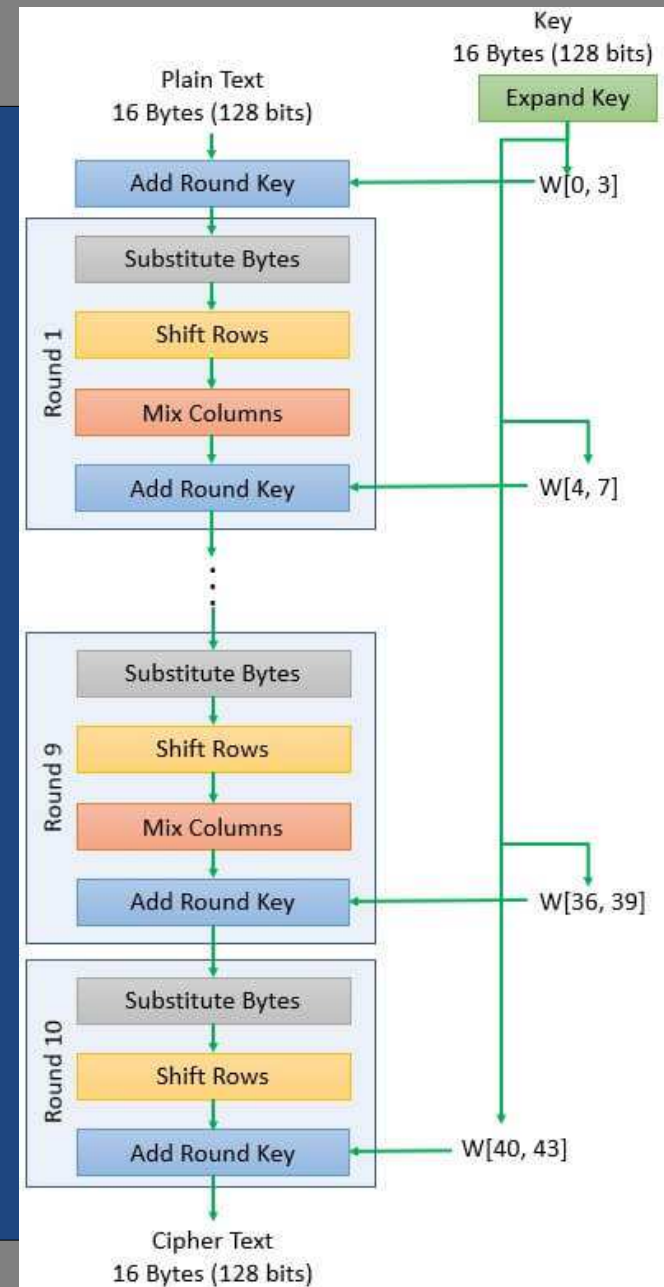
Private (Symmetric) Key Crypto



- One key:
 - ..
 - ..
 - This was the only type of encryption prior to invention of public-key in 1970's.

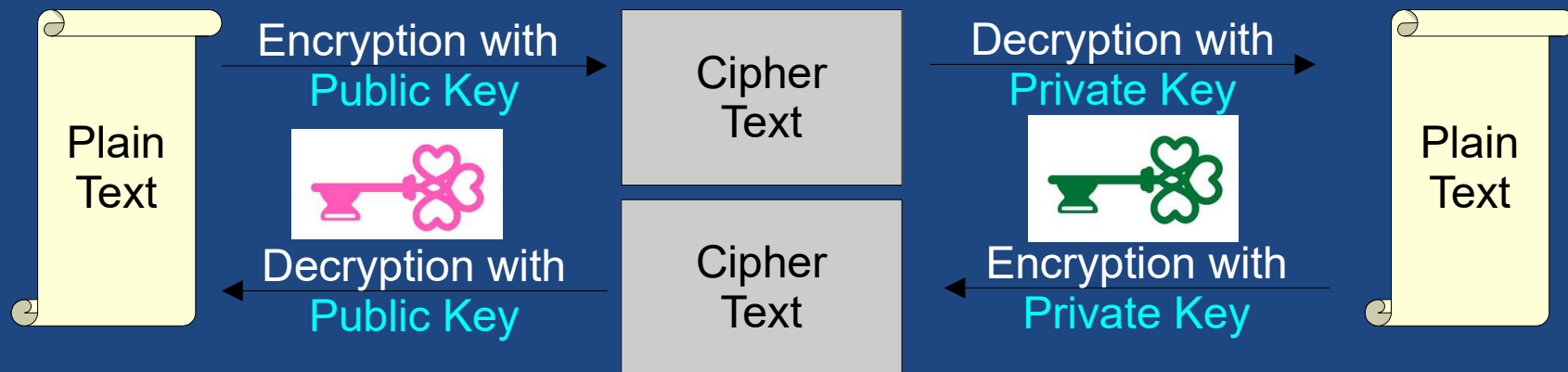
Private Key Crypto: AES

- AES is an **example private key crypto algorithm**
 - Need the same key to encrypt and decrypt.



Public Key Crypto or Asymmetric Crypto (Two keys)

Public Key Crypto (Asymmetric)



- There are two keys:
 - Public key: can be known to anybody
 - Used to encrypt and verify signatures (more below).
 - Private key: ..
 - Used to decrypt and sign signatures (more below).
- Fundamental property of public key encryption:
 - ..

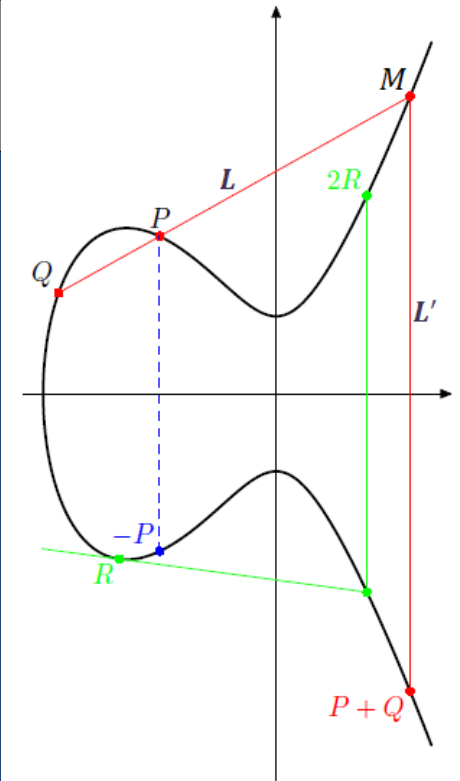
Toy Asymmetric Algorithm

- How does asymmetric encryption actually work?
- Key 1 and Key 2 are effectively an “inverse” of each other
 - ..
- Analogy to Caesar’s Cipher
 - Key 1: Encrypt by shifting letter to right by 7
 - Key 2: Decrypt by shifting letter to right by 19
 - Example: Message is “Hi”
A B C D E F G **H** I J K L M N **O** P Q R S T U V W X Y Z

 - H shifted right by 7 = O
 - O shifted right by 19 = H
 - We are always doing the same algorithm (toy is shifting right).

Generating Keys

- **Generating keys**
 - The public and private keys are ..
- **Example approaches to generating keys**
 - Factoring very large prime numbers,
 - Solving "Twisted Edwards curves" (ed25519)
- **Description of RSA algorithm**
<https://www.youtube.com/watch?v=qph77bTKJTM>
 - Uses simple numbers to show how it works. 8m



$$\begin{aligned} p & \cdot q \\ n &= pq \\ e & \text{ - coprime to } (p-1)(q-1) \\ c &= m^e \pmod{n} \\ c & \text{ is sent to me} \\ \text{Find } d & \text{ s.t. } de = 1 \pmod{(p-1)(q-1)} \\ m &= c^d \pmod{n} \end{aligned}$$

Keeping Secrets

- Example: Keeping Secrets
 - Alice wants to send a secret message to Bob
 - ..
 - Bob decrypts the cipher-text using his private key
- Analysis
 - Since only Bob knows Bob's private key, only Bob can decrypt the cipher-text.
 - Hence Alice and Bob can securely share the message.

Verifying Sender

- **Example: Verifying Sender**
 - Bob wants Alice to know that he sent a messages and it has not been altered.
 - ..
 - Alice decrypts the cipher-text using Bob's **public key**.
- **Analysis**
 - Since only Bob knows Bob's private key,
 - ..
 - Alice knows it was Bob who created the message.

Secret and Verified

- **Example: Secret and Verified**

Combine previous two examples.

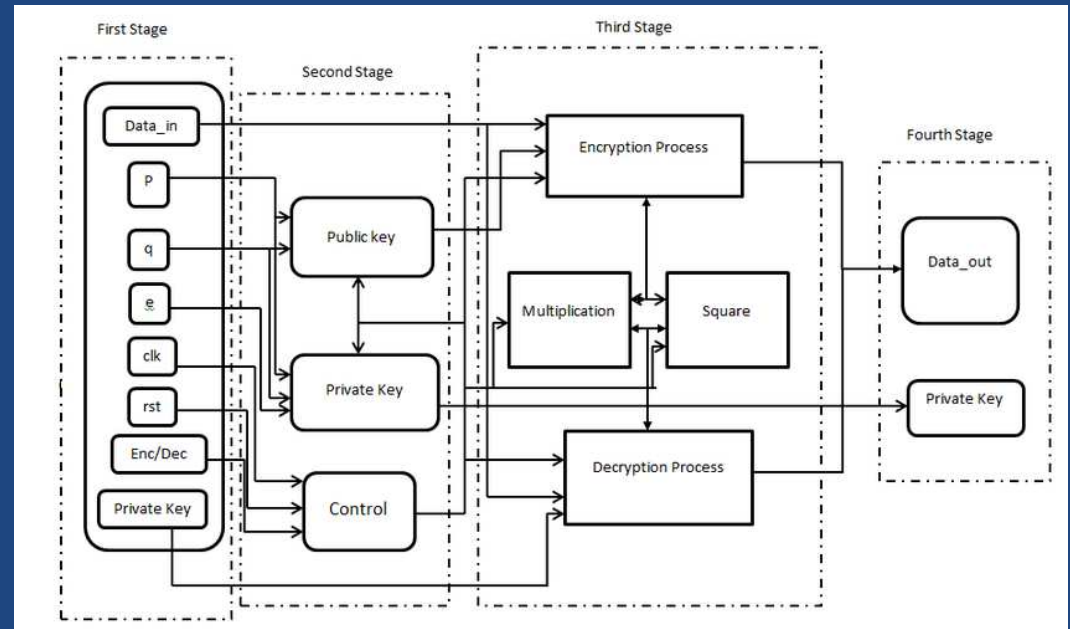
- Alice wants to send a verified, secret message.
- ..
 - Anyone can decrypt it with her public key.
 - But only she can encrypt with it; so we know she sent it!
- ..
 - Only Bob can decrypt it with his private key.

- **Analysis**

- Only Bob can decrypt the message (using his private key), and he'll know that only Alice can create it (using her private key).

Public Key

- **Benefit:**
 - This does not require having ..
 - Lots of other use cases beyond encryption / decryption
- **Example algorithm: RSA.**



Summary

- **Cryptography**
 - From **plain text**, create **cipher text** that others cannot read or change.
- **Types of algorithms**
 - 0 Keys: **Hash function**
 - 1 Key: **Symmetric encryption (private-key)**
 - Both sides know the **same secret key**.
 - 2 Keys: **Asymmetric encryption (public-key)**
 - You share a public key with the world.
 - Anyone can encrypt messages for you using this key.
 - **Only you can decrypt messages using your secret private key which matches the public key.**