

A close-up photograph of a person's hands working on a desk. The left hand holds a magnifying glass over a sheet of paper covered in a complex, repeating pattern of small, dark, geometric shapes. The right hand holds a pen, poised to write on an open notebook. The notebook has some faint, handwritten notes. The scene is dimly lit, with a strong light source from the left creating highlights on the paper and the person's hands. The overall atmosphere is one of focused investigation or research.

# Cryptography Algorithms

# Topics

- What is **cryptography**?
- What are the **basics of cryptographic algorithms**?
  - What are **cryptographic hashes**?
  - What is a **secret key encryption**?
  - What is **public-key encryption**?

# Cryptography: The absolute basics

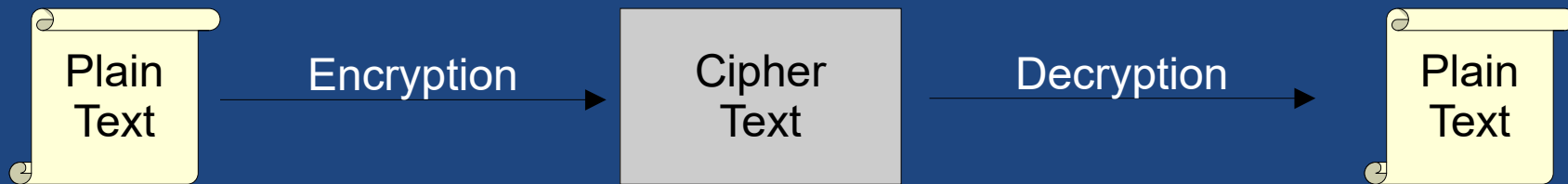
# Context

- **Cryptography**
  - A very broad area.
  - We'll focus on how to use cryptography.
  - We just touch on the basics!

# The CIA Model

- CIA model: the classic security model.
  - Confidentiality:  
..
  - Integrity:  
..  
and only by authorized parties.
  - Availability:  
..
- Threat examples
  - Against confidentiality: classified information leak
  - Against integrity: fake images/videos
  - Against availability: Denial-of-Service (DoS) attacks

# General Cryptography Process



- Cryptographers invented secret codes to hide messages from unauthorized observers.
- **Challenges:**
  - How can you **hide** a message from everyone but the intended recipient?
  - How can the recipient know the message is **authentic**?

# ABCD: Traditional Cryptography

- Traditional Cryptography:
  - Secret codes, which are secret algorithms.
  - E.g., Caesar Cipher: ..

For +1 'A' becomes 'B'.

- ABCD: Which of the following is the cipher text from using a 3-letter shift Caesar Cipher on the plain text "Hello world"?

- a) EBIIL TLOIA
- b) KH00R ZRU0G
- c) IFMMP XPSME
- d) LOW0R LDHEL

- What is the problem with a secret algorithm?
  - When your algorithm (or code book) is compromised,  
..

# Modern Encryption

- Algorithms are Public
  - ..
  - May be symmetric (secret key) or asymmetric (public key).
- Why is this better?
  - If algorithm or code is secret, then if it falls into the wrong hands it means code is useless.
  - If only key is private, then if it falls into the wrong hands then ..



# Crypto Algorithm Goals

- Choose an encryption algorithm such that:
  - Given a key, it should be  
..
  - Without a key, it should be  
..
- Strength of security often based on length of key:  
Longer key is more difficult to guess (by brute-force).

# Window of Validity

- Window of Validity
  - ..
  - Must only use algorithm that have not been compromised.
- Problem:  
Window of validity of your crypto function
  - ..
  - Design systems so you can replace the crypto function easily.
- Example Windows of Validity
  - 1993: SHA-0 was published.
  - 1995: Possible weakness was found in the SHA-0 algorithm; replaced with SHA-1.
  - 2004: Published way to compromise SHA-0
  - 2017: Published way to compromise SHA-1
  - ????: Published way to compromise SHA-256?

# Three Types

- Types of cryptography algorithms based on their keys:
  - Zero keys: ..
  - One key: ..
  - Two keys: ..

# Cryptographic Hash Functions (Zero Keys)

# Cryptographic Hash Functions

- Suppose we have a cryptographic hash function  $h()$ 
  - It takes a message  $m$  of arbitrary length as input and
  - ..

- Toy example:  
 $h(m) = (m^2) \% 4321$

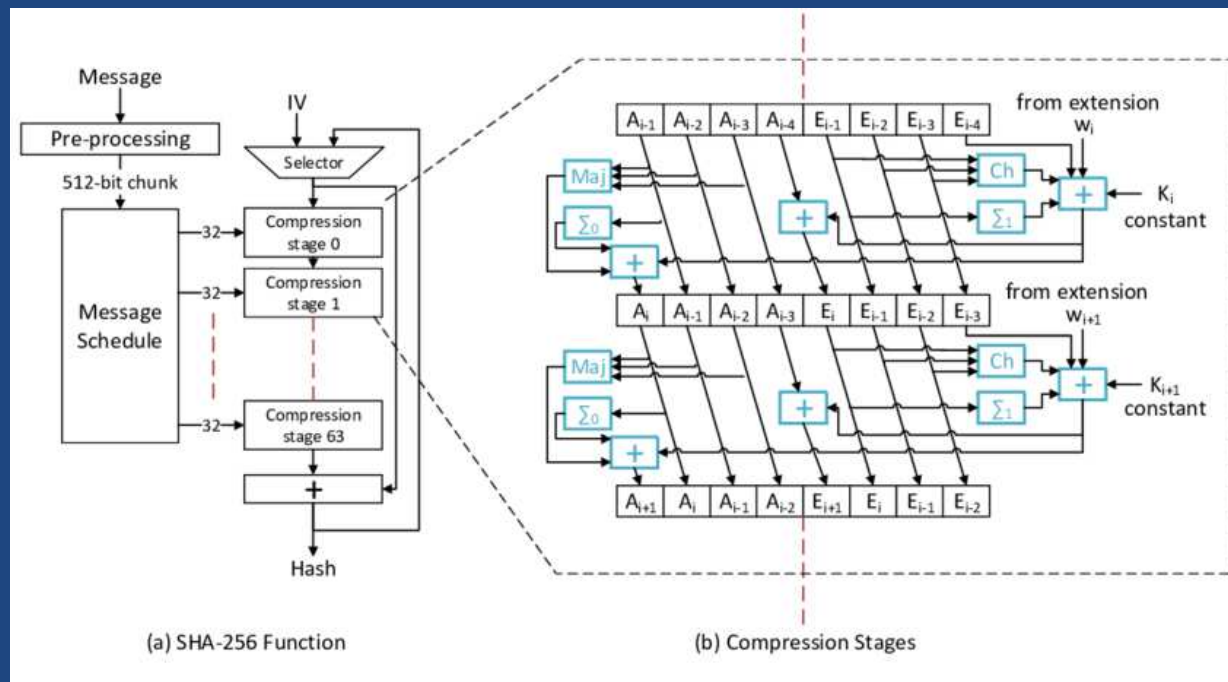
m	m in hex		h(m)
AAAA	(0x41414141)	-->	2242
BBBB	(0x42424242)	-->	893
CCCC	(0x43434343)	-->	2558
DDDD	(0x44444444)	-->	2916
EEEE	(0x45454545)	-->	1967
FFFF	(0x46464646)	-->	4032
GGGG	(0x47474747)	-->	469
HHHH	(0x48484848)	-->	4241
IIII	(0x49494949)	-->	2385
JJJJ	(0x4A4A4A4A)	-->	3543
KKKK	(0x4B4B4B4B)	-->	3394
LLLL	(0x4C4C4C4C)	-->	1938

# Hash Function Properties

- ..
  - It should be easy to compute  $h(m)$
- ..
  - Given  $h(x)$ , it should be difficult to find  $x$ .
  - i.e., the reverse of  $h()$  should be difficult to compute.
- ..
  - Given  $x$ , it should be difficult to find  $x'$  where  $h(x') == h(x)$
  - i.e., Given a value and a hash function, it should be difficult to find another value that produces the same hash.
- ..
  - It should be difficult to find two messages  $x$  and  $x'$  where  $h(x) == h(x')$
  - i.e., given a hash function, it should be difficult to find two values that produce the same hash.

# Ideal Hash

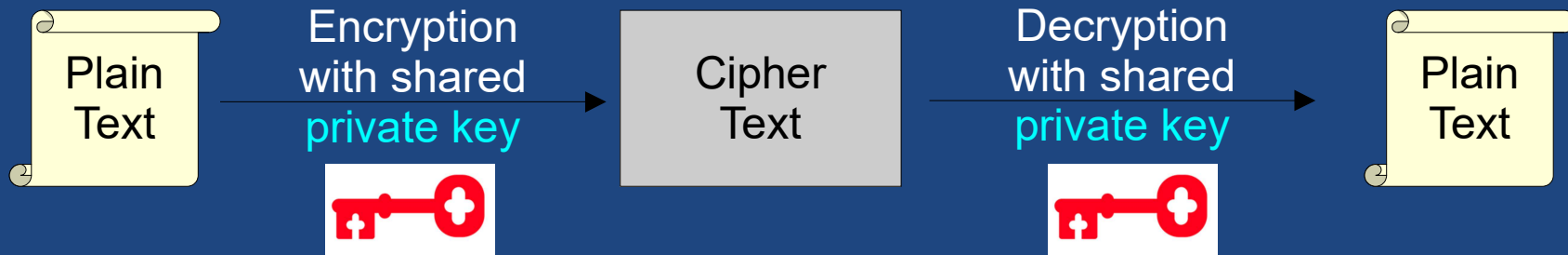
- Ideally, we want all these properties for a strong cryptographic hash function.
  - However, not all hash functions provide all these properties.
- Example good crypto hash function: SHA-256.



# Private Key Cryptography or Symetric Key Cryptography (One key)



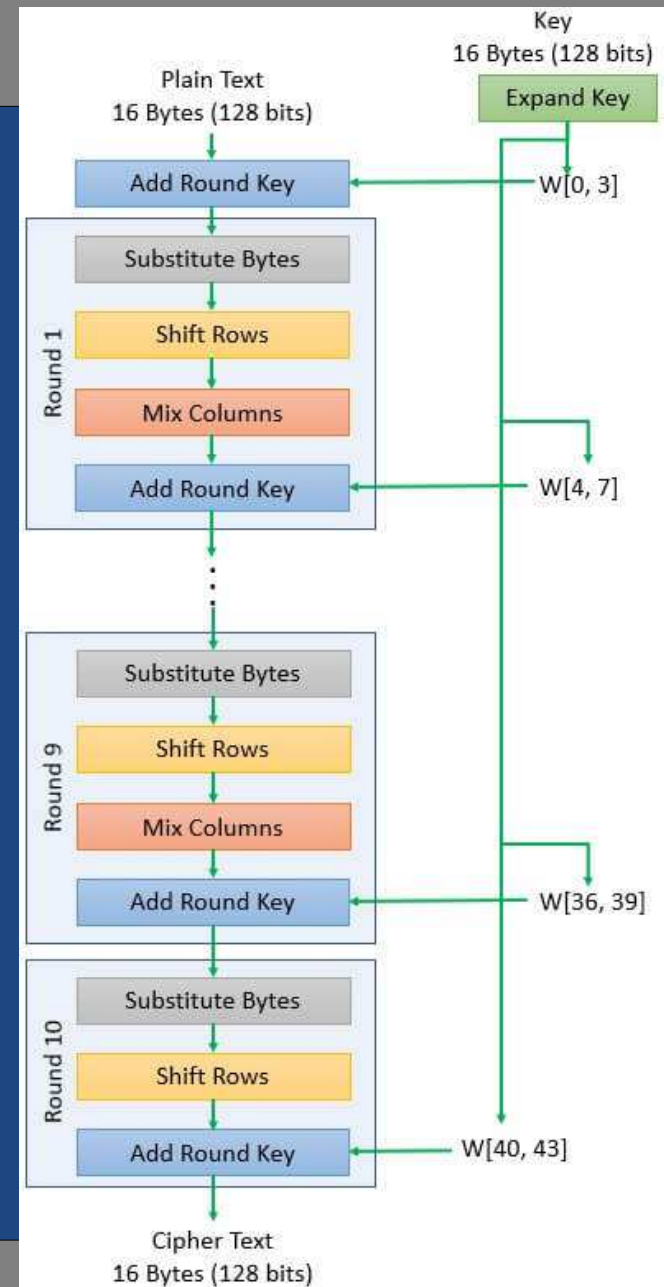
# Private (Symmetric) Key Crypto



- One key:
  - ..
  - ..
  - This was the only type of encryption prior to invention of public-key in 1970's.

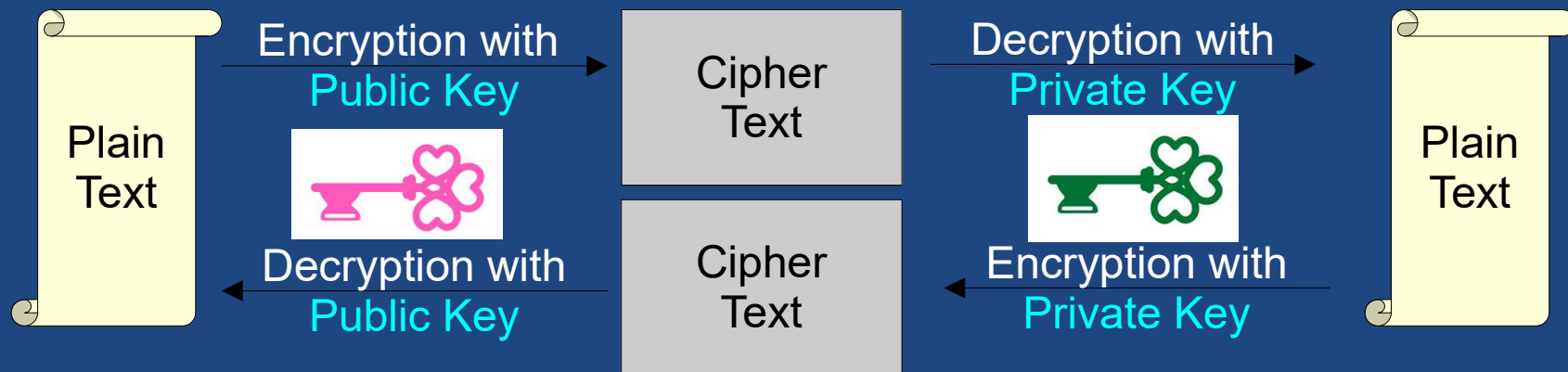
# Private Key Crypto: AES

- **AES** is an **example private key crypto algorithm**
  - Need the same key to encrypt and decrypt.



# Public Key Crypto or Asymmetric Crypto (Two keys)

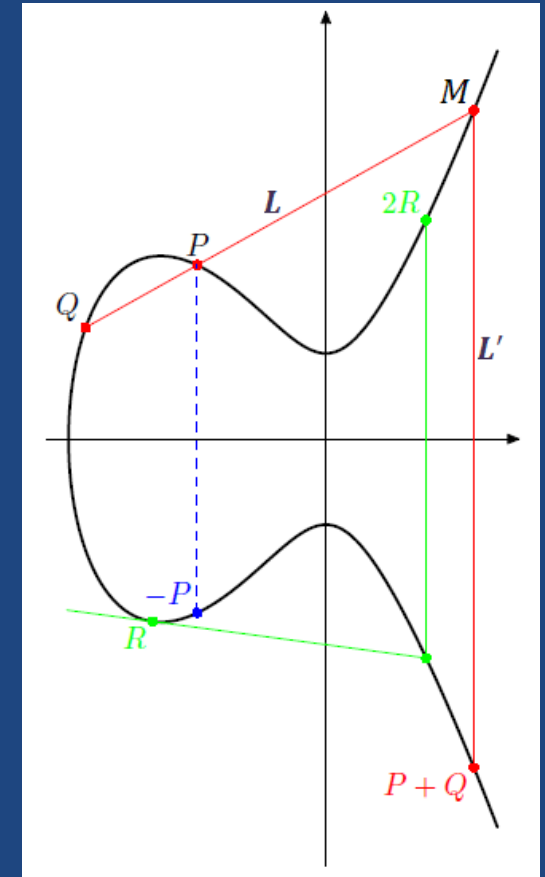
# Public Key Crypto (Asymmetric)



- There are two keys:
  - Public key: can be known to anybody
    - Used to encrypt and verify signatures (more below).
  - Private key: ..
    - Used to decrypt and sign signatures (more below).
- Fundamental property of public key encryption:
  - ..

# Generating Keys

- **Generating keys:**
  - The public and private keys are ..
- **Example approaches to generating keys**
  - Factoring very large prime numbers,
  - Solving "Twisted Edwards curves" (ed25519)



# Keeping Secrets

- **Example: Keeping Secrets**
  - Alice wants to send a secret message to Bob
  - ..
  - Bob decrypts the cipher-text using his **private key**
- **Analysis**
  - Since only Bob knows Bob's private key, only Bob can decrypt the cipher-text.
  - Hence Alice and Bob can securely share the message.

# Verifying Sender

- **Example: Verifying Sender**
  - Bob wants Alice to know that he sent a messages and it has not been altered.
  - ..
  - Alice decrypts the cipher-text using Bob's **public key**.
- **Analysis**
  - Since only Bob knows Bob's private key,
    - ..
  - Alice knows it was Bob who created the message.

# Secret and Verified

- **Example: Secret and Verified**

Combine previous two examples.

- Alice wants to send a verified, secret message.
- ..
  - Anyone can decrypt it with her public key.
  - But only she can encrypt with it; so we know she sent it!
- ..
  - Only Bob can decrypt it with his private key.

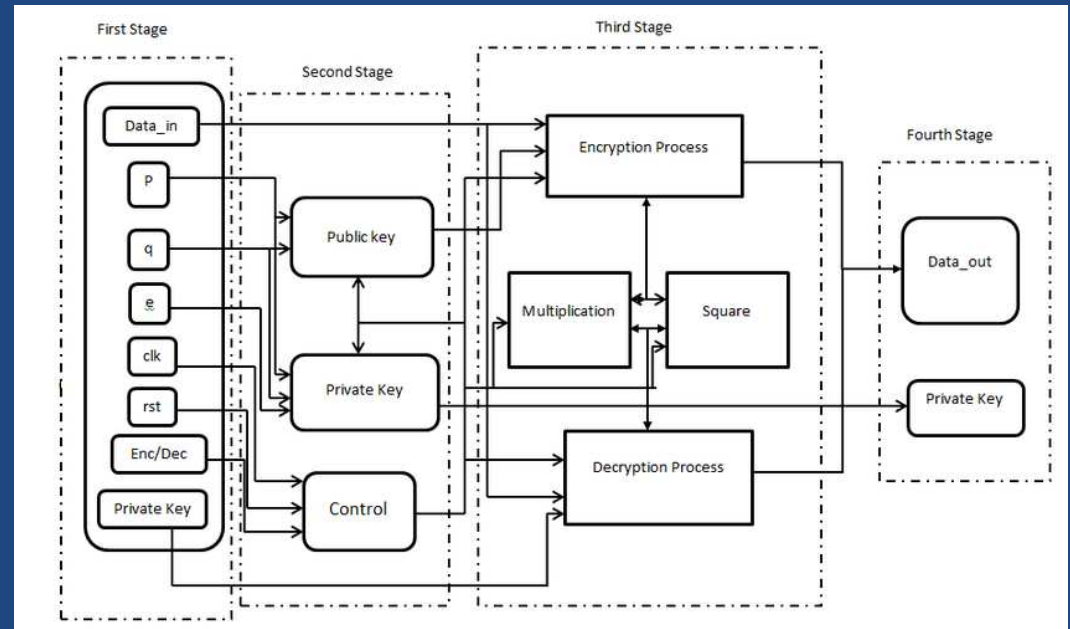
- **Analysis**

- Only Bob can decrypt the message (using his private key), and he'll know that only Alice can create it (using her private key).



# Public Key

- **Benefit:**
  - This does not require having ..
  - Lots of other use cases beyond encryption / decryption
- **Example algorithm: RSA.**



# Summary

- **Cryptography**
  - From **plain text**, create **cipher text** that others cannot read or change.
- **Types of algorithms**
  - 0 Keys:     **Hash function**
  - 1 Key:     **Symmetric encryption (private-key)**
    - Both sides know the **same secret key**.
  - 2 Keys:     **Asymmetric encryption (public-key)**
    - You share a public key with the world.
    - Anyone can encrypt messages for you using this key.
    - **Only you can decrypt messages using your secret private key which matches the public key.**