

Expressions

Chapter 2.3 (part)

Slides #4

$$6 - 1 \times 0 + 2 \div 2 = ?$$

ANSWER

IT



Topics

- 1) How can we calculate values?
- 2) What's the best way to work with values like 3600?

Math Expressions

(And not like "Wow! Math is great!")

Expressions

- Expression:
 - A statement that...
 - Usually has an operator.
- Examples:
 - result = 3;
 - result = x * 2;
 - result = 1 * x + 2;
- Expressions usable anywhere a value is needed:
 - cout << "Big number " << (1 + 2) << endl;

Order of Operations

- What is the value of result?
 `int result = 4 + 10 / 2;`
 - Is it 7 or 9? $(4 + 10) / 2$ or $4 + (10 / 2)$
- Each operator is given a precedence:
 - Higher precedence operators are applied first.
 - / is higher than +, so the answer is..
 - Add brackets to force an ordering.
- Associativity:
 - Apply the operators from right-to-left, or left-to-right?
 - +, - are left to right: do the one on the..
 - =, += are right to left: do the one on the..

Operator precedence

- Operators at same evaluated based on associativity.
 - * and / from L to R
 - = and += from R to L
- Examples:
 - result = -20 + 9 / 5;
 - result = (-20 + 9) / 5;
 - val = 6 + 5 * 4 / 3 * 2;
 - sum = sum + 10;

Prec. Level	Op.	Operation	Associates
1	[]	Array Index	L to R
2	+ -	unary plus unary minus	R to L
3	* / %	mult, div, remainder	L to R
4	+ -	add subtract	L to R
5	<< >>	stream ins. extract.	L to R
6	< <= > >=	comparisons	L to R
7	= += -= *=	assignments	R to L
	...		

Order can be forced by parentheses.
See text Appendix 2 for full table.

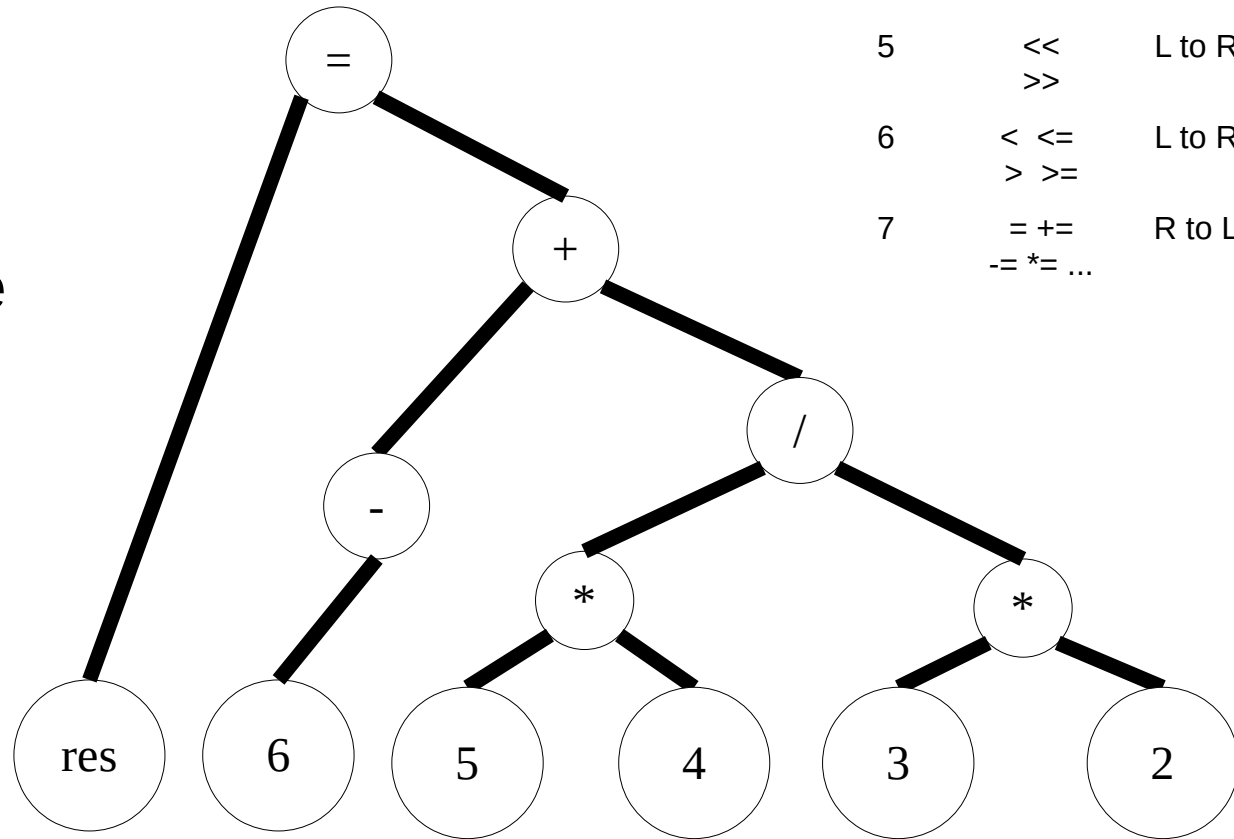
Brackets

- A statement can be correct, but unreadable:
 - $\text{result} = 1 + 2 / 6 - 1 * 3 / 4 - 3 - -3 * +4;$
- Add brackets to make it clear:
 - $\text{result} = 1 + (2 / 6) - (1 * 3 / 4) - 3 - ((-3) * (+4));$

Expression tree

Prec. Level	Op.	Asso.
1	[]	L to R
2	unary + unary -	R to L
3	* / %	L to R
4	+ -	L to R
5	<< >>	L to R
6	< <= > >=	L to R
7	= += -= *= ...	R to L

- Represent $res = (-6 + 5 * 4 / (3 * 2))$ as a tree:
- Operands as leaves.
- Operators as branching nodes.
- Operations lower in the tree have..
- Evaluate from the..
- Write values on internal nodes.



Review

- Draw an expression tree for the following:

answer = $5 * x + 6 * (1 - x);$

Assume $x=2$

Prec. Level	Op.	Asso.
1	[]	L to R
2	unary + unary -	R to L
3	* / %	L to R
4	+ -	L to R
5	<< >>	L to R
6	< <= > >=	L to R
7	= += -= *= ...	R to L

Constants

Constants

- We have already used literal constants:

```
int x = 10;           // Numeric constant  
cout << "Hello world!\n"; // String literal
```
- Raw number in code are..

```
int w = d / 7;  
int c = s / 72;
```
- Use named constants like variables:

```
const int MIN_PER_HOUR = 60;  
int h = m / MIN_PER_HOUR;
```

const

- **const** qualifier makes variable...

```
const int PAY_PER_DAY = 475;  
const int DAYS_PER_WEEK = 7;
```

 - Constants must be given a value when created.
 - Name is upper case by..
 - Program cannot modify value of a constant:

```
PAY_PER_DAY = 99999; // ERROR!
```
- **Advantages:**
 - Program becomes more...
 - Can change value in entire program in one spot.
 - Ex: change tax rate that's used in 100 calculations!

Example with const

```
// Convert days to weeks/years/fortnights.
// #includes/uses... omitted for space.
const int DAYS_PER_WEEK = 7;
const int DAYS_PER_YEAR = 365;

int main()
{
    const int DAYS_PER_FORTNIGHT = 14;

    cout << "Enter # days: ";
    int numDays = 0;
    cin >> numDays;

    int numWeeks = numDays / DAYS_PER_WEEK;
    int numYears = numDays / DAYS_PER_YEAR;
    int numFortnight = numDays / DAYS_PER_FORTNIGHT;

    cout << "# Days:      " << setw(4) << numDays << endl;
    cout << "# Weeks:     " << setw(4) << numWeeks << endl;
    cout << "# Years:      " << setw(4) << numYears << endl;
    cout << "# Fortnights: " << setw(4) << numFortnight << endl;
}
```



Constants can be..

```
Enter # days: 4641
# Days:      4641
# Weeks:     663
# Fortnights: 331
```

Guide to Constants

- Which of the following literal constants would be best made into named constants?
 - `int numStudents = 0;`
 - `int next = numStudents + 1;`
 - `int waitlist = numStudents – 72;`

Combined Assignments & Overflow

Assignment Operators

- Combine an operation with assignment:

- +=, -=, *=, /=, %=

- Examples:

- a += b;
// means a = a + b;

- a *= b;
// means a = a * b;

- a /= 2 + 3;
// means...

```
const int MAX_COUNT = 10;
int main()
{
    ..
    int sum = 0;
    int i = 0;
    while (i < MAX_COUNT) {
        sum += i;
        i++;
    }
    cout << "Sum from 0 to "
         << MAX_COUNT - 1
         << " = " << sum << endl;
}
```


Overflow & Underflow

- Each type has a maximum value it can store.
 - Maximum + 1 overflows to the most negative.
 - Minimum – 1 underflows to the most positive.

```
// Work with overflow/underflow
```

```
#include <iostream>
```

```
#include <climits>
```

```
using namespace std;
```

```
int main()
```

```
{  
    int test = INT_MAX;  
    cout << "Test starts out at: " << test << endl;  
    test += 1;  
    cout << "Adding one gives us: " << test << endl;  
    test -= 1;  
    cout << "Now subtracting 1: " << test << endl;  
}
```

```
Test starts out at: 2147483647
```

```
Adding one gives us: -2147483648
```

```
Now subtracting 1: 2147483647
```

#include <climits>..

INT_MAX, INT_MIN,
CHAR_MAX, CHAR_MIN,
....

Suggested Review Questions

- Draw an expression tree for the following:
result = $8 * -1 + 3 / 2$
 - Solve it by writing values on the nodes.
 - Write a C++ program to double check your answer.

Summary

- Expressions calculate values using operators.
 - Operator precedence gives us expression trees.
- Use named constants (const), not magic numbers.
- Combined assignment operators like `x += 2;`